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## ON GPS- NAVIGATION

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On GPS- navigation STARIKOV V. N., Isachenkov F.N. Michurinsk State Teachers Training Institute It is classic problem (the different-distance-method) for determination of unknown Cartesian object-coordinates  $x, y, z$  in known instant  $t$  of earthly objects using known Cartesian 4 or 5 satellite-coordinates  $x_i, y_i, z_i$ ,  $i=1,2,3$  in the same time  $t$  or their measured object-distances  $r_i = \sqrt{(x_i - x)^2 + (y_i - y)^2 + (z_i - z)^2}$ ,  $i=1,2,3,4,5$ . Problem reduced to solved system of 3-equations in 3 unknowns:  $AX=b$ ,  $X=(x,y,z)^T$  - unknowns-vector,  $b$  - known constants-vector,  $A$  -  $3 \times 3$ - matrix of known coefficients depending on  $x_i, y_i, z_i$  or  $r_i$ ,  $i=1,2,3,4$  for  $dr=0$ . Here  $c$  is unknown constant for object-distance-measurement-error to satellites  $r_i$ . This error depend on time-nonsynchronization of object-clock and satellites.clock,  $c$  is light-velocity in vacuum. Problem reduced to solved system of 4-equations in 4 unknowns:  $AX=b$ ,  $X=(x,y,z,dr)^T$  - unknowns-vector,  $b$  - known constants-vector,  $A$  -  $4 \times 4$ - matrix of known coefficients depending on  $x_i, y_i, z_i$  or  $r_i$ ,  $i=1,2,3,4,5$  for  $dr>0$ . It is proved theorem. This theorem consequence consist on that it need 4-5 coplanar satellites sometimes or 2 and more crossing-orbits-satellites in order to measure  $r_i$  - distances to object for neighbouring instants:  $t, t+dt, t+2dt$ . Formulae are coded as in  $\text{\LaTeX}$  or  $\text{\AMS-TeX}$ .